

Long-Term Continuously Updated Deformation Time Series from Multi-Sensor InSAR in Xi'an, China from 2007 to 2021

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Abstract—According to historical records, land subsidence has been occurring in Xi'an, China since the 1960s, characterized by complex land subsidence patterns. This subsidence has the potential to cause serious societal and economic problems during the process of urbanization. Long-term, large-scale monitoring and dynamic high precision tracking of the evolution of surface deformation associated with geohazards is a prerequisite for effective prevention or advance warning of geological disasters. Synthetic aperture radar interferometry (InSAR), a satellite remote sensing technology, can facilitate such monitoring. Both currently operating and planned SAR satellites will provide extensive amounts of SAR data. In this paper, we describe an approach for continuously updating long-term multi-sensor InSAR deformation time series using robust sequential least squares. It is successfully applied to near-real-time monitoring of the long-term evolution of surface deformation in Xi'an, China from January 3, 2007 to February 12, 2021 using four SAR satellites: ALOS/PALSAR-1, TerraSAR-X, ALOS/PALSAR-2, and Sentinel-1A. In order to analyze deformation evolution, temporal independent component analysis was used to interpret deformation patterns. We found that land subsidence in Xi'an has slowed and even halted in some areas. However, large areas are uplifting, which presents a potential for geohazards. We conclude that the proposed approach using continuously updated deformation time series from multi-sensor InSAR can provide near-real-time deformation measurements, which are necessary for an early warning system.

Index Terms— Multi-sensor InSAR, robust sequential least squares, surface deformation update, independent component analysis,

I. INTRODUCTION

INTERFEROMETRIC synthetic aperture radar (InSAR) is playing an increasingly critical role in investigating deformation of the Earth's surface. Over the last 30 years,

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InSAR has been used to reconstruct historical surface deformation [1] and has been successfully used to monitor the surface deformation caused by various geohazards such as earthquakes [2], volcanoes [3], landslides [4], and land subsidence [5].

During urbanization, land subsidence in urban areas can seriously damage surrounding buildings, reducing safety and causing significant societal and economic harm. InSAR technology can investigate surface deformation over large scales and with high precision. It has been used to investigate surface deformation in Las Vegas [6] and Houston–Galveston, USA [7], Mexico City, Mexico [8], northeast Iran [9], the West Thessaly Basin, Greece [10], the Pisa Urban area, Italy [11], and Beijing [12], amongst others. Over-exploitation of groundwater is a principal cause of land subsidence.

In the last few decades, several multi-temporal InSAR (Mt-InSAR) algorithms have been developed [13–23], which can be divided into two main families. The first group is based on the single-master permanent scatterer (PS) InSAR technique [13], which uses highly reflective objects (e.g., human-made infrastructure in urban areas) that preserve high coherence and phase stability even in large temporal and perpendicular baseline SAR data pairs. The second group comprises multiple-master small baseline subset (SBAS) InSAR techniques [14] that use distributed scatterers (DSs), which are distributed over resolution cells at multiple resolutions and are characterized by varying coherence and phase stability. Expanded PS and SBAS algorithms have been developed for deformation time series analysis, and are described in detail in [24] and [25]. Correct identification of DSs and phase optimization is required, for which several techniques have been proposed [26]. When applying InSAR technology to long-term continuous land subsidence investigation and time series analysis, the SBAS technique can mitigate the effects of decorrelation by the short-temporal-space baseline interferogram pair, especially in regions suffering from heavy decorrelation, a large deformation gradient, and a long time horizon. Thus, it is well-suited to investigate long-term surface deformation. The onboard SAR satellites (Sentinel-1A/B, ALOS/PALSAR-2, TerraSAR-X/TanDEM-X, COSMO-SkyMed, and Radarsat-2), in combination with planned SAR satellites, will provide a significant quantity of data and shortened intervals between revisits. Using multiple sensors to investigate surface deformation, affords two outcomes. The first is a two-dimensional or three-dimensional surface deformation

rate, and a resulting deformation time series. The second is the ability to fuse the deformation rate or the deformation time series with higher temporal resolution. In previous studies, combined multi-sensor SAR data have been used to monitor land subsidence [27], volcano deformation [28], and landslides [29]. Other applications of multi-sensor, multi-track, and multi-dimensional deformation are summarized in [30] and [31].

The fusion of multi-sensor SAR data to rapidly estimate deformation time series can improve the frequency of deformation time series production, which facilitates obtaining early warning of disasters. To this end, parallel computation and cloud computing were used to accelerate processing of InSAR data [32]. The Kalman filter has been used to update deformation time series [33] [34]; however, inaccurate deformation prediction information can easily lead to deviations in deformation time series. The sequential filtering method was developed to optimize DS phase and avoid computational burden using full interferograms [35]. Sequential SAR data registration [36] [37] has been proposed for Sentinel-1 TOPSAR images. Sequential least squares (SLS) and complex SLS (CSLS) methods have been used to dynamically update deformation parameters for single SAR sensors, including line-of-sight (LOS) deformation time series [38] and two-dimensional offset tracking deformation time series [39], without the loss of accuracy as compared with conventional SBAS-InSAR and PO-SBAS (Pixel offset SBAS), respectively.

In this era of massive and diverse SAR data availability, how can we process multi-sensor SAR data simultaneously and provide deformation time series as quickly and precisely as possible? We propose a robust sequential least squares

(RSLS) algorithm, which processes multi-sensor SAR data simultaneously to dynamically update, and improve the temporal resolution of, deformation time series. Fusing multi-sensor SAR data can assist in providing early warning of disasters.

In this study, using vertical deformation as seen in land subsidence/uplift as an example, we devised an approach to continuously update multi-sensor InSAR deformation time series in order to monitor in near-real-time the long-term evolution of surface deformation in Xi'an, China. We applied the approach over a 13-year study period from January 3, 2007 to February 12, 2021, using four SAR satellites. In order to analyze deformation evolution, temporal independent component analysis was used to interpret deformation patterns. We focus on time series analysis and found that the land subsidence rate in Xi'an is slowing, with a future trend of uplift deformation.

II. STUDY AREA AND DATA

A. Study Area

Xi'an is located to the north of the Qinling Mountains, in the vicinity of the Loess Plateau in China. It is bounded by the Chan River and Ba River to the east, the Feng River to the west, and the Wei River to the north. Loess ridges and depressions are interchangeably distributed in central urban areas (Fig. 1).

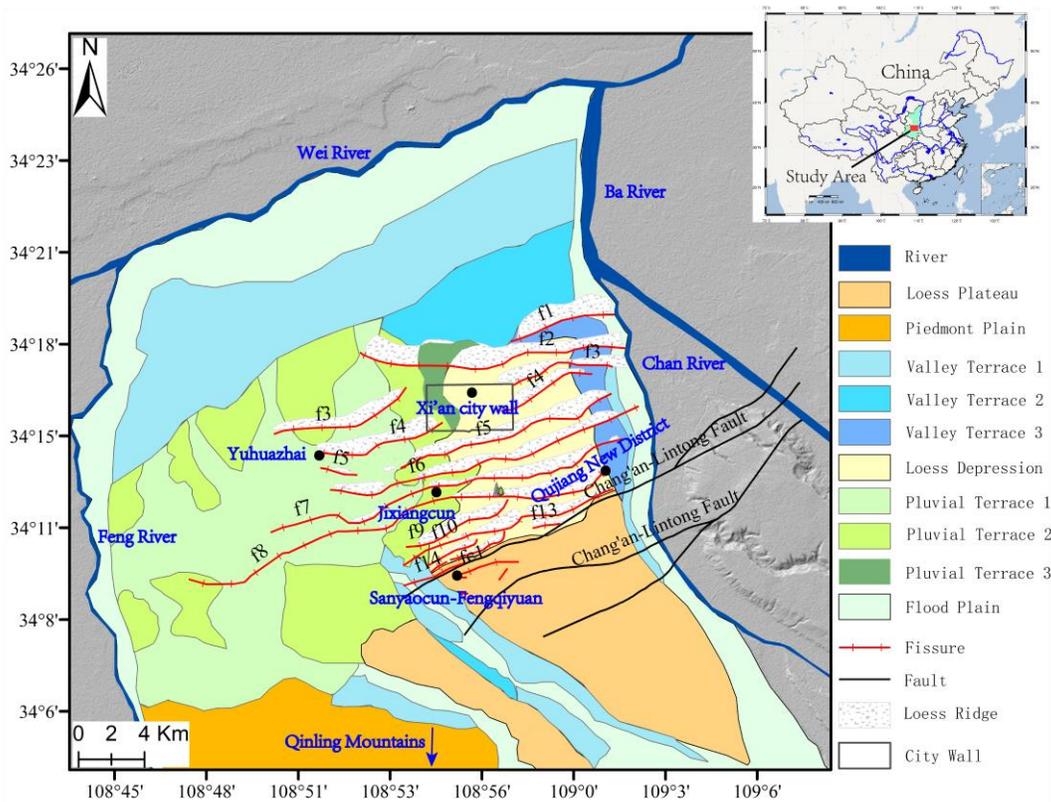


Fig. 1. Quaternary geology map of Xi'an [40].

Since the 1960s, Xi'an has suffered from severe land subsidence and ground fissure hazards [41]. Economic development and urbanization have led to more than 50 years of excessive groundwater exploitation [41]. Subsequently, 14 ground fissures formed, accompanied by land subsidence [42]. The Chang'an-Lintong fault (CAF), which runs mainly in the ENE direction, controls the activities of the 14 ground fissures. The interaction between these fissures and land subsidence areas has developed into elliptical-shaped surface subsidence [43].

Large scale InSAR data have been used to investigate the spatiotemporal characteristics of subsidence and ground fissures in Xi'an. These include Global Positioning System (GPS) and InSAR observations from 2005 to 2006 [44]; Envisat, ALOS, and TerraSAR SAR datasets from 2005 to 2012 [45]; ERS, Envisat, and Sentinel SAR datasets from

2003 to 2017 [46]; ALOS, TerraSAR, and Sentinel SAR datasets from 2012 to 2018 [47]; and Sentinel SAR datasets from 2015 to 2019 [40]. These studies showed that degradation of the aquifer system had led to complex subsidence and ground fissures.

B. Satellite SAR Data

Our study used 192 SAR images, including 22 from ALOS/PALSAR-1 with $4.6 \text{ m} \times 3.1 \text{ m}$ in range and azimuth (from January 30, 2007 to February 10, 2011), 46 from TerraSAR-X with $0.9 \text{ m} \times 1.8 \text{ m}$ (from October 5, 2011 to 28 May 2015), 9 from ALOS/PALSAR -2 with $4.2 \text{ m} \times 3.2 \text{ m}$ (from September 6, 2014 to October 28, 2017), and 115 from Sentinel-1A with $2.3 \text{ m} \times 13.9 \text{ m}$ (from June 20, 2015 to February 12, 2021) (Fig. 2).

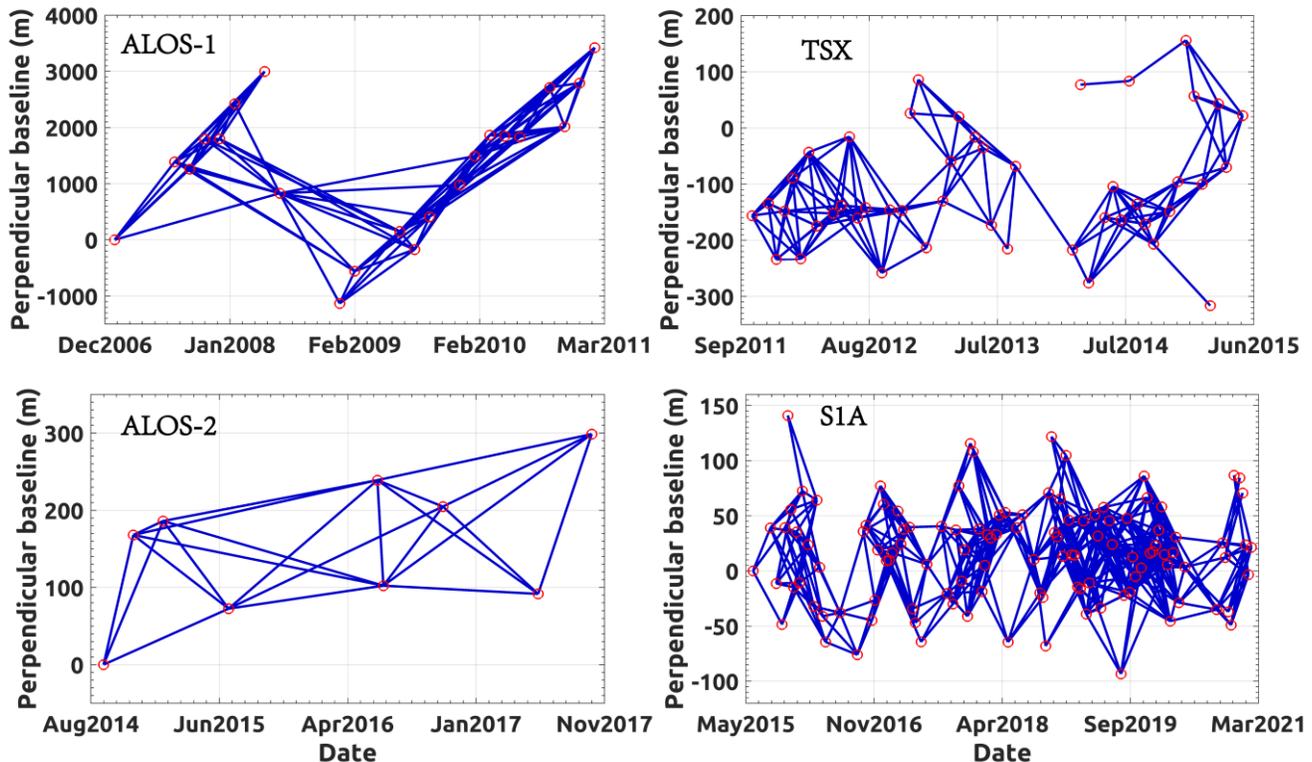


Fig. 2. Temporal and perpendicular baseline map of data from four synthetic aperture radar (SAR) sensors used in this study.

III. METHODOLOGY

A. Updating Multi-Sensor InSAR Deformation Time Series

Phase unwrapping of interferogram is a key step in InSAR data processing [18,21,48,49]. Yu et al. [50] reviewed the progress of InSAR phase unwrapping. After correcting digital elevation model (DEM) error, atmospheric artifacts, and orbital error for unwrapped interferograms, we used the L1-norm approach to alleviate the gross error caused by phase unwrapping, using $V_1 = A_1 X - L_1$, P_1 , in which V_1 is the measurement noise; A_1 is the design matrix with -1, 0, and 1; L_1 is the measurement data (unwrapped interferograms); and P_1 is the weight matrix. This can be solved using the iteratively reweighted least squares (IRLS) method with the equivalent weight matrix \bar{P}_1 [51]. The deformation time series is dynamically updated using $X^{(1)} = (A_1^T \bar{P}_1 A_1)^{-1} A_1^T \bar{P}_1 L_1$ and $\bar{Q}_{X^{(1)}} = (A_1^T \bar{P}_1 A_1)^{-1}$ as the parameter X and its cofactor matrix for archived data, respectively.

Once we obtain a new SAR image, we firstly form interferograms by combining the new SAR image with recent past acquisitions. Using the SBAS strategy, we extract common pixels (as archived data) to produce phase unwrapping and error correction. Then, we have a new observation L_2 (unwrapped interferograms). To estimate parameters X and Y , we model the new observation with the design matrixes A_2 and B , and weight matrix P_2 as in (1):

$$V_2 = [A_2 \quad B] \begin{bmatrix} X^{(2)} \\ Y \end{bmatrix} - L_2, \quad P_2 \quad (1)$$

where $X^{(2)}$ and Y are the new estimation of parameter X and cumulative deformation, respectively, at the new SAR acquisition date.

Similarly, the L1-norm approach, $\arg \min \|V_2\|_1$ is used to determine the weight matrix \bar{P}_2 in order to alleviate the gross error in (1). The number of newly unwrapped interferograms in (1) is usually small, which is likely to lead to an ill-conditioned problem. According to the principle of least squares Bayesian estimation theory [52], it holds that

$$V_2^T \bar{P}_2 V_2 + (X^{(2)} - X^{(1)})^T \bar{Q}_{X^{(1)}}^{-1} (X^{(2)} - X^{(1)}) = \min \quad (2)$$

Therefore, we can take $X^{(1)}$ and $\bar{Q}_{X^{(1)}}$ as *a priori* information of the estimated parameter $X^{(2)}$ to calculate the equivalent weight matrix \bar{P}_2 and update the deformation time series $[X^{(2)} \quad Y]^T$ and its cofactor matrix $\bar{Q}_{[X^{(2)}, Y]}$ as follows [38].

$$\begin{bmatrix} X^{(2)} \\ Y \end{bmatrix} = \begin{bmatrix} \bar{Q}_{X^{(1)}}^{-1} + A_2^T \bar{P}_2 A_2 & A_2^T \bar{P}_2 B \\ B^T \bar{P}_2 A_2 & B^T \bar{P}_2 B \end{bmatrix}^{-1} \begin{bmatrix} \bar{Q}_{X^{(1)}}^{-1} X^{(1)} + A_2^T \bar{P}_2 L_2 \\ B^T \bar{P}_2 L_2 \end{bmatrix}$$

$$\bar{Q}_{[X^{(2)}, Y]} = \begin{bmatrix} \bar{Q}_{X^{(1)}}^{-1} + A_2^T \bar{P}_2 A_2 & A_2^T \bar{P}_2 A_2 \\ B^T \bar{P}_2 A_2 & B^T \bar{P}_2 B \end{bmatrix}^{-1} \quad (3)$$

To avoid obtaining a large-scale inverse matrix, we use matrix inversion theory [38] [53] to solve (3):

$$\begin{aligned} \begin{bmatrix} \mathbf{X}^{(2)} \\ \mathbf{Y} \end{bmatrix} &= \begin{bmatrix} \mathbf{X}^{(1)} + \mathbf{J}_x (\bar{\mathbf{L}}_2 - \mathbf{B} \mathbf{Y}) \\ (\mathbf{B}^T \bar{\mathbf{Q}}_J^{-1} \mathbf{B})^{-1} \mathbf{B}^T \bar{\mathbf{Q}}_J^{-1} (\mathbf{L}_2 - \mathbf{A}_2 \mathbf{X}_1) \end{bmatrix} \\ \bar{\mathbf{Q}}_{[\mathbf{X}^{(2)}, \mathbf{Y}]} &= \begin{bmatrix} \bar{\mathbf{Q}}_{\mathbf{X}^{(2)}} & \bar{\mathbf{Q}}_{\mathbf{X}^{(2)}, \mathbf{Y}} \\ \bar{\mathbf{Q}}_{\mathbf{X}^{(2)}, \mathbf{Y}}^T & \bar{\mathbf{Q}}_{\mathbf{Y}} \end{bmatrix} \\ \bar{\mathbf{Q}}_{\mathbf{X}^{(2)}} &= \bar{\mathbf{Q}}_{\mathbf{X}^{(1)}} - \mathbf{J}_x \mathbf{A}_2 \bar{\mathbf{Q}}_{\mathbf{X}^{(1)}} + \mathbf{J}_x \mathbf{B} \bar{\mathbf{Q}}_{\mathbf{Y}} \mathbf{B}^T \mathbf{J}_x^T \\ \bar{\mathbf{Q}}_{\mathbf{X}^{(2)}, \mathbf{Y}} &= -\mathbf{J}_x \mathbf{B} \bar{\mathbf{Q}}_{\mathbf{Y}, \mathbf{Y}} \\ \bar{\mathbf{Q}}_{\mathbf{Y}} &= (\mathbf{B}^T \bar{\mathbf{Q}}_J^{-1} \mathbf{B})^{-1} \\ \mathbf{J}_x &= \bar{\mathbf{Q}}_{\mathbf{X}^{(1)}} \mathbf{A}_2^T \bar{\mathbf{Q}}_J^{-1} \\ \bar{\mathbf{Q}}_J &= \bar{\mathbf{P}}_2^{-1} + \mathbf{A}_2 \bar{\mathbf{Q}}_{\mathbf{X}^{(1)}} \mathbf{A}_2^T \end{aligned} \quad (4)$$

where $[\mathbf{X}^{(2)}; \mathbf{Y}]$ is the updated deformation time series, and $\bar{\mathbf{Q}}_{[\mathbf{X}^{(2)}, \mathbf{Y}]}$ is their cofactor matrix.

This technique for updating deformation time series is executed for data from additional sensors in turn. Assuming purely vertical deformation, such as when monitoring for land subsidence, there will be overlapping time periods of data measured from multiple sensors. After determining the multi-sensor deformation time series, we can project various deformations in the LOS direction to the vertical direction

$$D_{Def}^i = \frac{X_{Los}^i}{\cos(\varphi^i)},$$

in which i represents different SAR sensors,

D_{Def} is the vertical deformation time series, and φ is incidence angle. X_{Los} is the deformation time series in the LOS direction. Next, we project multi-sensor deformation time series into the geographic coordinate system, and resample the different resolution deformation time series into the same one. We extract the common monitoring points of all sensors, pixel by pixel, to fuse the deformation time series. Specifically, we generate the deformation time series by adjusting the systematic deviation between two different sensors in the overlapping periods. We model the deviation as follows:

$$\begin{aligned} (\mathbf{X}_1 - d) - \mathbf{X}_2 &= \mathbf{V} \\ \mathbf{V}^T \mathbf{P} \mathbf{V} &= \min \\ \Delta \mathbf{X} &= \mathbf{M} d + \mathbf{V}, \quad \mathbf{P} \end{aligned} \quad (5)$$

$$d = (\mathbf{M}^T \mathbf{P} \mathbf{M})^{-1} \mathbf{M}^T \mathbf{P} \Delta \mathbf{X} = \frac{1}{n} \sum_{i=1}^n (\mathbf{X}_{1,i} - \mathbf{X}_{2,i})$$

where \mathbf{X}_1 and \mathbf{X}_2 are the overlapping deformation time series from multi-sensor SAR data, \mathbf{V} is the residual deformation, d is the systematic deviation between two deformation time series, and \mathbf{M} is the design matrix. We used least squares criteria to fuse deformation time series within the overlapping periods, which is similar to using quantile adjustment with a cumulative distribution function [54] and overlapping data [55], to correct system deviations. Fig. 3 shows the flow chart of the automatic multi-sensor InSAR deformation time series.

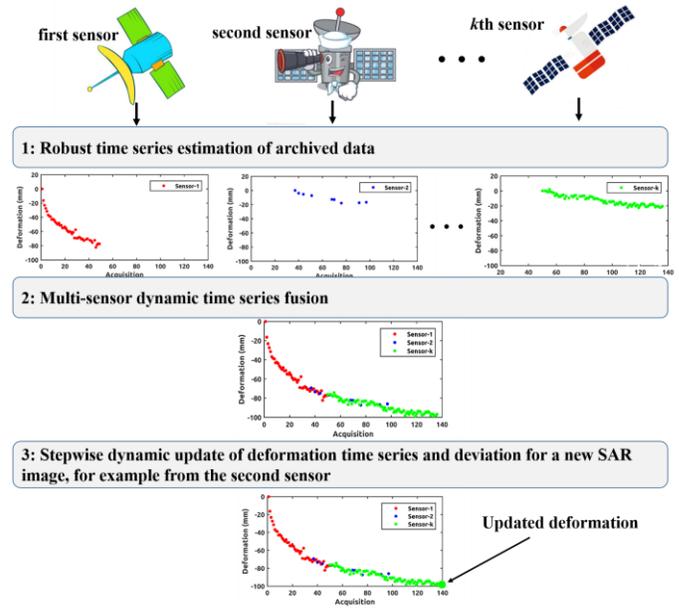


Fig. 3. Flowchart showing continuous updating of multi-sensor synthetic aperture radar interferometry (InSAR) deformation time series.

In cases with no horizontal deformation, we use the correct datum of overlapping data among each sensor/track to fuse one-dimensional vertical deformation time series. Otherwise, we use multi-sensor, multi-track deformation time series to update multi-dimension deformation time series as follows:

$$\begin{bmatrix} \cos \theta_1 & -\sin \theta_1 \cos \alpha_1 \\ \cos \theta_2 & -\sin \theta_2 \cos \alpha_2 \end{bmatrix} \begin{bmatrix} D_V t_n \\ D_E t_n \end{bmatrix} = \begin{bmatrix} D t_{n1} \\ D t_{n2} \end{bmatrix} \quad (6)$$

where D_V and D_E are vertical and east-west deformation, θ_1 and α_1 are incident angle and heading angle, respectively, of the first sensor or track data, and θ_2 and α_2 are incident angle and heading angle, respectively, of the second sensor or track data. The t represents the n th observation. t_{n1} and t_{n2} indicate the first and second sensor or track LOS cumulative deformation. It is straightforward to extend the three-dimensional deformation time series through the inclusion of additional observation data [30] [31].

B. Temporal-ICA-Based Spatiotemporal Deformation Pattern Decomposition

Once we have obtained the long-term deformation time series over a larger area, we must determine how to identify different complex deformation characteristics. The different characteristics of InSAR-driven ground deformation time series have been studied using independent component analysis (ICA). This method was introduced in [56] and relies on the assumption that the observed ground deformation signal can be factorized as a linear combination of statistically independent components. ICA has been used to separate atmospheric noise from signals [57], and to better understand elastic deformation [58], DEM error [59], and volcanic

deformation [60]. The unique solution is derived by maximizing the mutual independence of estimating each statistically independent component.

Temporal ICA (tICA) assumes that terrain deformation signal sources are temporally, statistically independent. In order to separate different spatiotemporal deformation patterns over large scales, tICA maximizes the statistical independence of an arbitrary number of independent components (ICs), and fits different temporal patterns and spatial functions [57].

To apply tICA, we first re-organized the obtained ground deformation time series related to the set of np pixels well-processed, coherent SAR pixels as $\mathbf{U} = [\Phi_1^{def}, \Phi_2^{def}, \dots, \Phi_{np}^{def}]^T$ with $\Phi^{def} = [\phi_0^{def}, \phi_1^{def}, \dots, \phi_{N-1}^{def}]$. Each row of \mathbf{U} represents the relevant ground deformation time series values and each column represents the selected coherent SAR pixels. We used the FastICA algorithm [61] [62] with a temporal model to decompose the mixed-signal matrix \mathbf{U} into a set of ns statistically independent sources in the temporal $\mathbf{S} = [s_1, s_2, \dots, s_{ns}]^T$ ($s_i = [s_i^0, s_i^1, \dots, s_i^{N-1}]$) and mixing $\mathbf{A} = [a_1, a_2, \dots, a_{ns}]$ ($a_i = [a_i^1, a_i^2, \dots, a_i^{np}]^T$) matrixes, in which \mathbf{S} and \mathbf{A} are unknown. In the FastICA algorithm, fixed-point iteration is employed to derive the converged solution of the mixing matrix \mathbf{A} and source matrix \mathbf{S} by maximizing the spatial non-Gaussianity of sources [59]. The mixing matrix \mathbf{A} captures the relative contribution of each independent temporal component. Accordingly, we modeled the ground deformation time-series as

$$\mathbf{U} = \mathbf{A}\mathbf{S} \quad (7)$$

In particular, it can be shown that the relationship between a set of deformation time series \mathbf{U} and the independent sources \mathbf{S} of a whole study area can be expressed as

$$\mathbf{U} = \sum_i^{ns} a_i \times s_i \quad (8)$$

where s_i is the spatial distribution of the i th independent source, and a_i is the vector of the relative contribution of corresponding source s_i . Therefore, we can use (8) for each spatial source and deformation time series.

IV. RESULTS AND ANALYSIS

A. Updating Multi-Sensor Deformation Time Series

In this study, the terrain-related atmospheric phase was removed from the best-fitting linear relation between the phase delay and topography [63,64]. The Generic Atmospheric Correction online service for InSAR (GACOS) [65] is a practical method for removing atmospheric phase. DEM error-caused phase was estimated using the relationship between perpendicular baseline and phase $\frac{4\pi}{\lambda} \frac{B^\perp}{\sin \theta} \Delta H = unw$ [66], where ΔH , and unw are DEM error and unwrapped interferometric phases, respectively. λ ,

R , and θ are the radar wavelength, sensor-to-target distance, and incidence angle, respectively. B^\perp is the perpendicular baseline. After correction of DEM error, atmospheric artifacts, and orbital error in the unwrapped interferograms, we used IRLS to produce deformation time series for each set of archived sensor data. At this stage, we stored deformation time series and their cofactor matrixes for post-processing. In the case of vertical deformation, we projected LOS direction deformations from different sensors to the vertical direction and geocoded them in the same geographical coordinate system. Finally, we fused the multi-sensor deformation time series using overlapping data to generate long-term and high temporal resolution deformation time series.

When new SAR data become available, we are able to generate new interferograms utilizing the new SAR image and the most recently archived SAR images originating from the same sensor, by setting short temporal and spatial baseline thresholds. Subsequently, we update the deformation time series for each newly acquired SAR image using (4). Fig. 4 shows the cumulative vertical deformation map obtained by fusing SAR data acquired from four different sensors between January 3, 2007 and February 12, 2021 and continuously updating the multi-sensor InSAR deformation time series. The data include 22 ALOS/PALSAR-1 images, 46 TerraSAR-X images, 9 ALOS/PALSAR-2 images, and 115 Sentinel-1A SAR images. The maximum land subsidence is more than 1.3 meters, and several areas of subsidence can be clearly seen between two ground fissures. The reference point is the black pentagram indicated in Fig. 4.

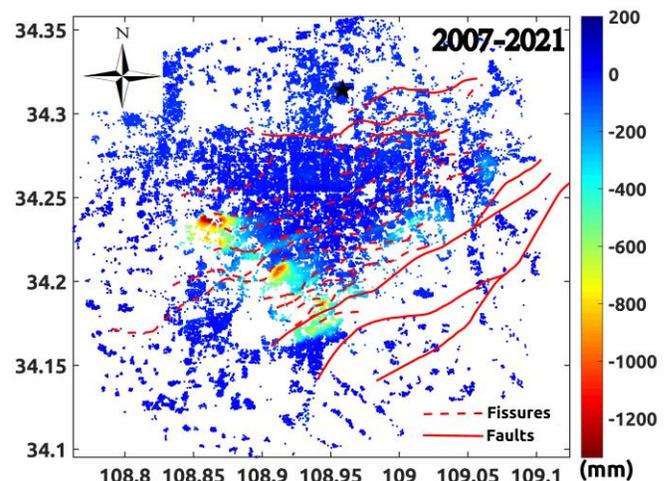


Fig. 4. Cumulative deformation from January 3, 2007 to February 12, 2021 obtained from continuously updated multi-sensor InSAR deformation time series from four SAR sensors. Black pentagram is reference point.

We introduce a method to continuously update multi-sensor InSAR deformation time series. It can dynamically process SAR datasets from single sensors and link different deformation time series from multiple sensors simultaneously. In addition, gross errors are effectively resolved using RLS. Therefore, the proposed method is an extension of sequential least square estimation.

Unlike linear interpolation [67], when using the overlapped

deformation to fuse and link different sensors or track deformation time series, the atmospheric error, orbit error, and DEM error phase should be corrected. Only Gaussian noise is permitted in deformation time series. Therefore, RLS is recommended.

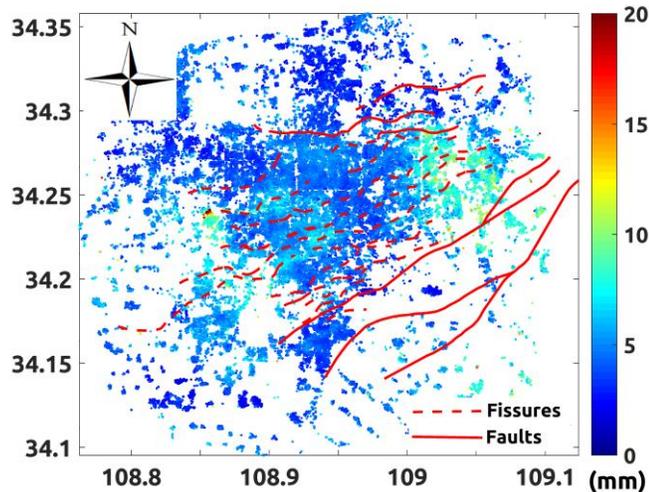


Fig. 5. Standard deviation of deformation time series of different SAR sensors in the overlapping time periods.

In order to analyze the accuracy of the deformation time series, we estimate the standard deviation (SD) of deformation time series from different sensors in overlapping time periods as shown in Fig. 5. Specifically, we used 9 ALOS/PALSAR-2 images and overlapping data in TerraSAR-X images and Sentinel-1A SAR images to estimate the SD. Different SAR sensor wavebands have different sensitivity to deformation, so their measurement accuracy differs. The SD between them is within 20 mm. Cross validation results of deformation time series obtained by different sensors proves that our estimated deformation time series are reliable.

B. Spatiotemporal Deformation Pattern Analysis

Previous research has mapped ground deformation characteristics using different sensors and across different time spans [40, 44-47]. With our newly developed continuously updating multi-sensor InSAR deformation time series approach, we were able to map the evolution of long-term surface deformation in Xi'an from January 3, 2007 to February 12, 2021, which is well suited to large-scale, near-real-time monitoring.

In order to map evolution characteristics and spatiotemporal scope, we used the tICA algorithm [61] [62] to investigate spatiotemporal evolution of Xi'an surface deformation from January 3, 2007 to February 12, 2021. The tICA assumes that the source signal is temporally independent in order to fit the spatiotemporal deformation characteristics. We assumed that there are four independent patterns of temporal evolution deformation. Principal component analysis (PCA) was used to explore the reliability of our hypothesis of four independent components, as shown in Fig. 6. The eigenvalues of the first four components can explain approximately 80% (70.1%,

6.7%, 2.8%, 1.4%) of the cumulative signal variance.

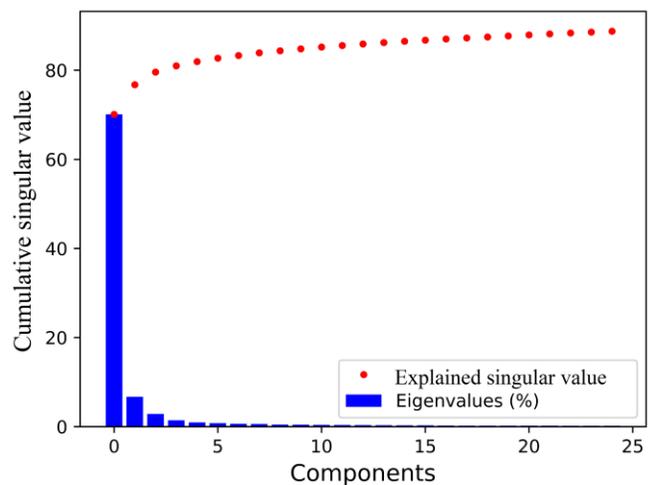


Fig. 6. Variance explained by each component in principal component analysis (PCA).

Then, the FastICA algorithm [61] [62] was employed to decompose the mixed-signal matrix stacking deformation time series \mathbf{U} with dimensions of 66380×192 (wherein 66380 represents the number of selected coherent pixels and 192 represents the number of SAR images) into a set of four statistically independent sources in temporal $\mathbf{S} = [s_1, s_2, s_3, s_4]^T$ ($s_i = [s_i^0, s_i^1, \dots, s_i^{191}]$) (Fig. 7) and mixing $\mathbf{A} = [a_1, a_2, a_3, a_4]$ ($a_i = [a_i^1, a_i^2, \dots, a_i^{66380}]^T$) matrixes (Fig. 8). In the FastICA algorithm, fixed-point iteration is used to derive the converged solution of mixing matrix \mathbf{A} and source matrix \mathbf{S} by maximizing the temporal non-Gaussianity of sources [59].

The temporal source matrixes s_1 (IC1), s_2 (IC2), s_3 (IC3), and s_4 (IC4) in Fig. 7 show four independent patterns of deformation evolution over time. The mixing matrixes a_1 , a_2 , a_3 , and a_4 capture the relative contribution of the independent temporal components a_1 (IC1), a_2 (IC2), a_3 (IC3), and a_4 (IC4), respectively (Fig. 8). Thus, there are four spatial deformation areas with different time evolution characteristics.

IC1 mapped the rebound deformation characteristics upon ceasing groundwater exploitation and the effect of the subsequent artificial water injection, as seen in the uplift at point A in Fig. 9. This is distinct from a rebound area in Xi'an introduced in [40]. Instead, IC1 mapped the spatial range of rebound deformation in Yuhazhai, well south and west of Xi'an.

In terms of temporal evolution, IC2 maps a deformation pattern of land subsidence and uplift around Jixiangcun. However, it is irregular in space and controlled by ground fissures. The three points B, C, and D were selected in IC2 to show deformation time series in Fig. 9.

IC3 mapped regions in Sanyaocun-Fengqiuyan and Qujiang New District that are experiencing subsidence, where the deformation rate gradually slows over the study period. The two points E and F were selected in IC3 to show deformation time series in Fig. 9.

The temporal deformation pattern in IC4 shows that no deformation was found from 2007 to 2011, at which point a linear deformation feature began, and continues to the present. The two points G and H were selected in IC4 to show deformation time series in Fig. 9.

In IC2, points B, C, and D show the same deformation time series pattern at the same magnitude (Fig. 9). However, in IC3

and IC4, we can see the influence of the CAF in the patterns of deformation time series evolution. Areas to the north (Fig. 9, point E) and south (Fig. 9, point G) of the fault show different temporal deformation patterns. In IC3, it is difficult to separate the two similar time deformation characteristics at points E and F.

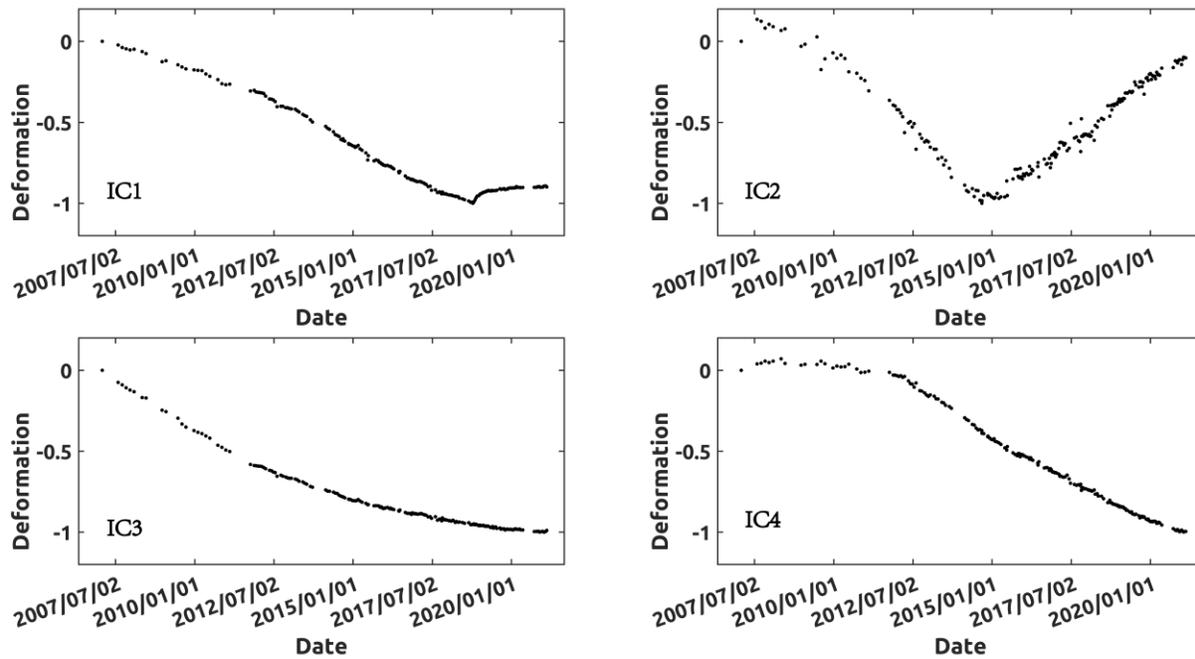


Fig. 7. Four different temporal deformation patterns, IC1 to IC4, obtained by independent component analysis.

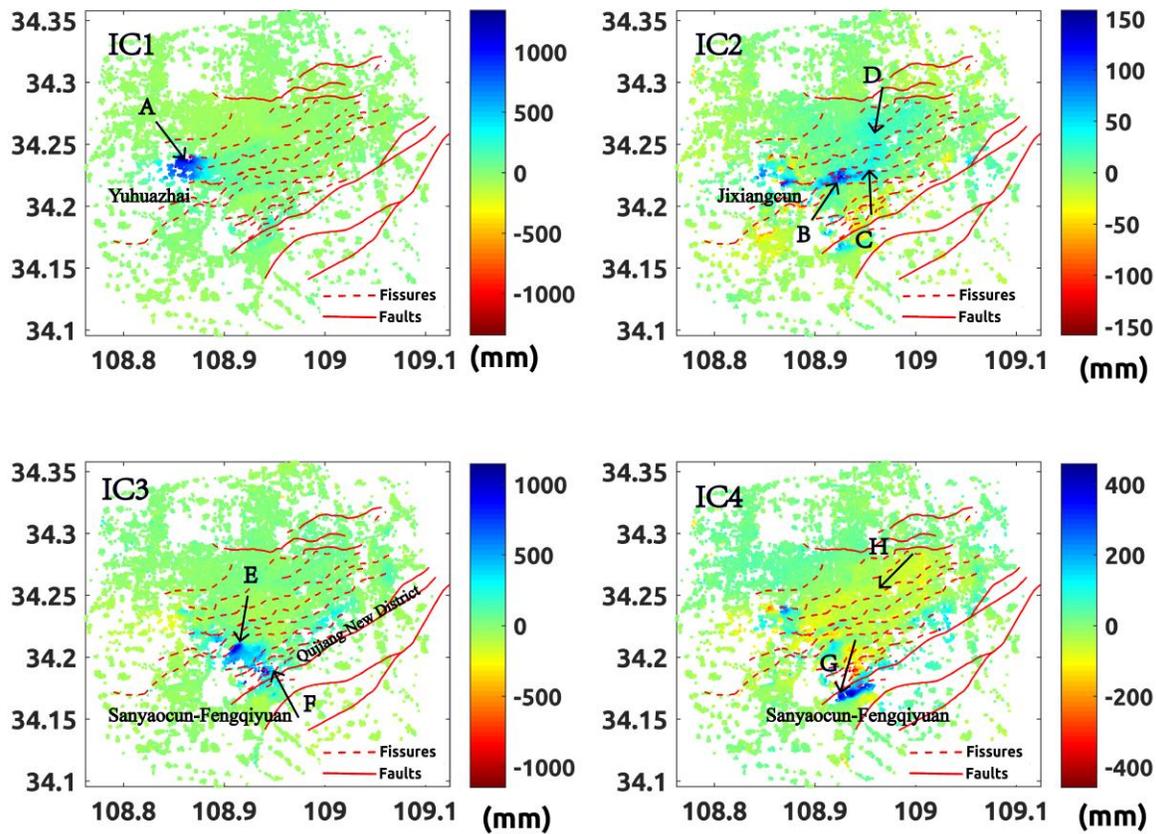


Fig. 8. Four different spatial deformation patterns, IC1 to IC4, obtained by independent component analysis. Points indicated by arrows A-H are shown in Fig. 9.

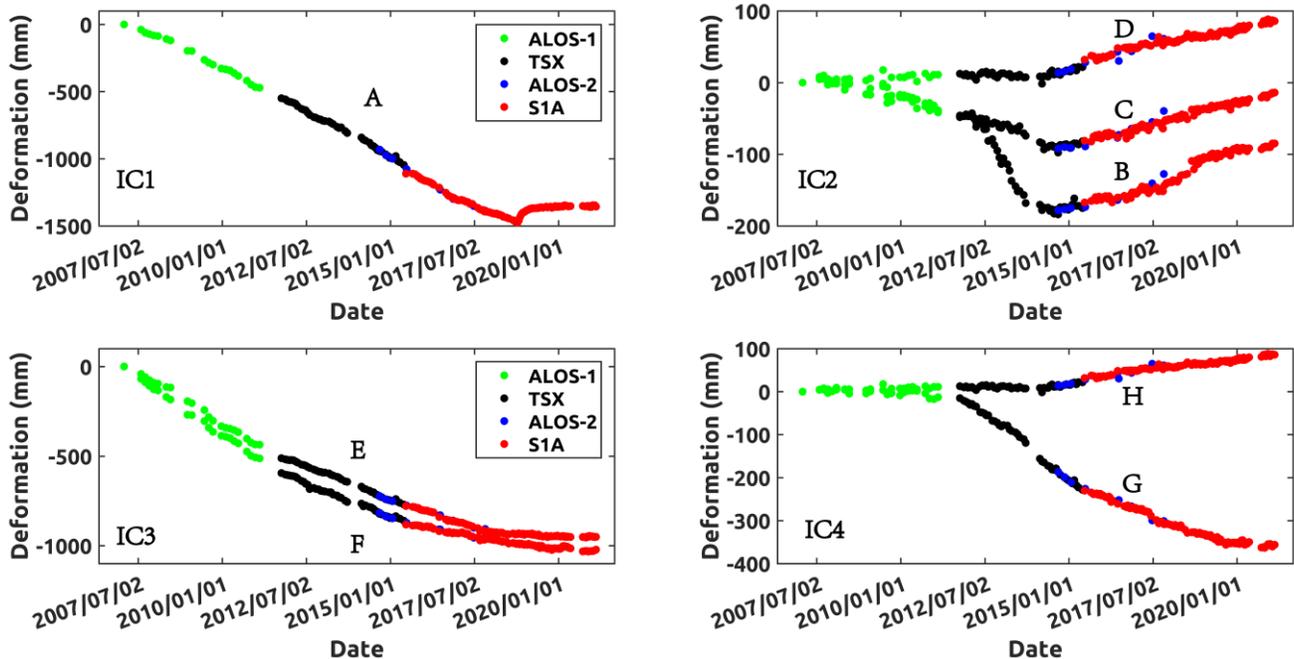


Fig. 9. Time series deformation A-H. The eight points were selected according to their spatial deformation patterns to show evolution of temporal deformation from January 3, 2007 to February 12, 2021.

C. Future Deformation Trends

Large-scale exploitation of confined water in Xi'an since the 1970s can be divided into three stages: exploitation,

over-exploitation, and cessation [43]. The main areas of land subsidence have experienced three stages: initial subsidence, serious subsidence, and then gradual stability [68]. Before 1970, the confined water level depth was 10-20 m. The land

subsidence area located in the east of Xi'an had a slow average subsidence rate of 2 mm per year. Between 1970 and 1995, due to economic development and urbanization, groundwater over-exploitation increased rapidly to over 1000 pumping wells, leading to an increase in confined water level depth of approximately 100 meters. As surface subsidence rates increased, the subsidence area expanded rapidly to the south of Xi'an, concentrated in the area of the Second Ring Road. During this period, regional subsidence centers and seven ground fissures were discovered.

From 1996 to 2002, groundwater exploitation was restricted in order to alleviate land subsidence, and the confined water level depth began to slowly move closer to the surface. Land subsidence within the Second Ring Road gradually slowed, and the subsidence center moved to the south. Thirteen ground fissures were found. Over-exploitation of groundwater leads to decreases in groundwater level. Although the confined aquifer is elastic, continuous over-exploitation of groundwater can lead to irrevocable confined aquifer deformation, which further leads to land subsidence [69].

Beginning in 2002, the primary water source for the region transitioned from subsurface withdrawal to water from the Heihe River and its associated dam projects. A cumulative water volume of 1 552 800 m³ was recharged to the subsurface between 2002 and 2017. By 2015, the water level rose to a depth of 90-100 m, and land subsidence began to slow. When groundwater exploitation stops and the confined aquifer water level recovers, land subsidence does not stop immediately; rather, after a period of continuous subsidence, it stops or rebounds. The deformation pattern can be divided into

immediate elastic recovery deformation and time-dependent visco-elastic recovery deformation [69].

We mapped the rate of deformation over the last two years (Fig. 10; the rectangular range represents the city wall of Xi'an). It is clear that the extent of the area of uplift deformation is great. The uplift deformation boundary in the south is controlled by ground fissures.

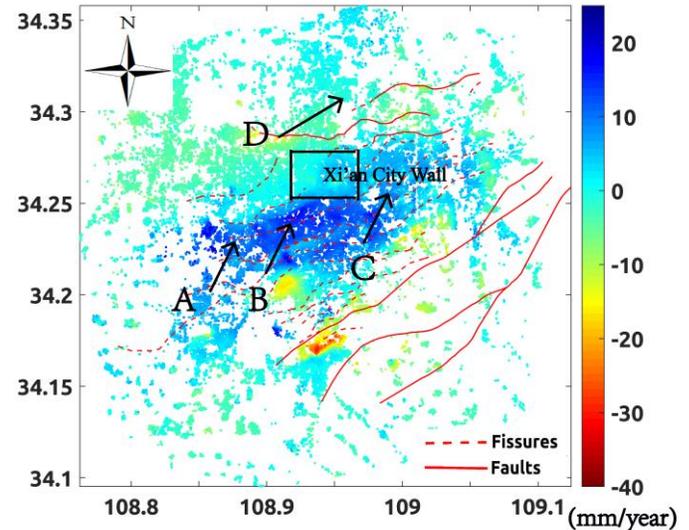


Fig. 10. Deformation rate from 2019 to 2021. Points A-D are shown in Fig. 11.

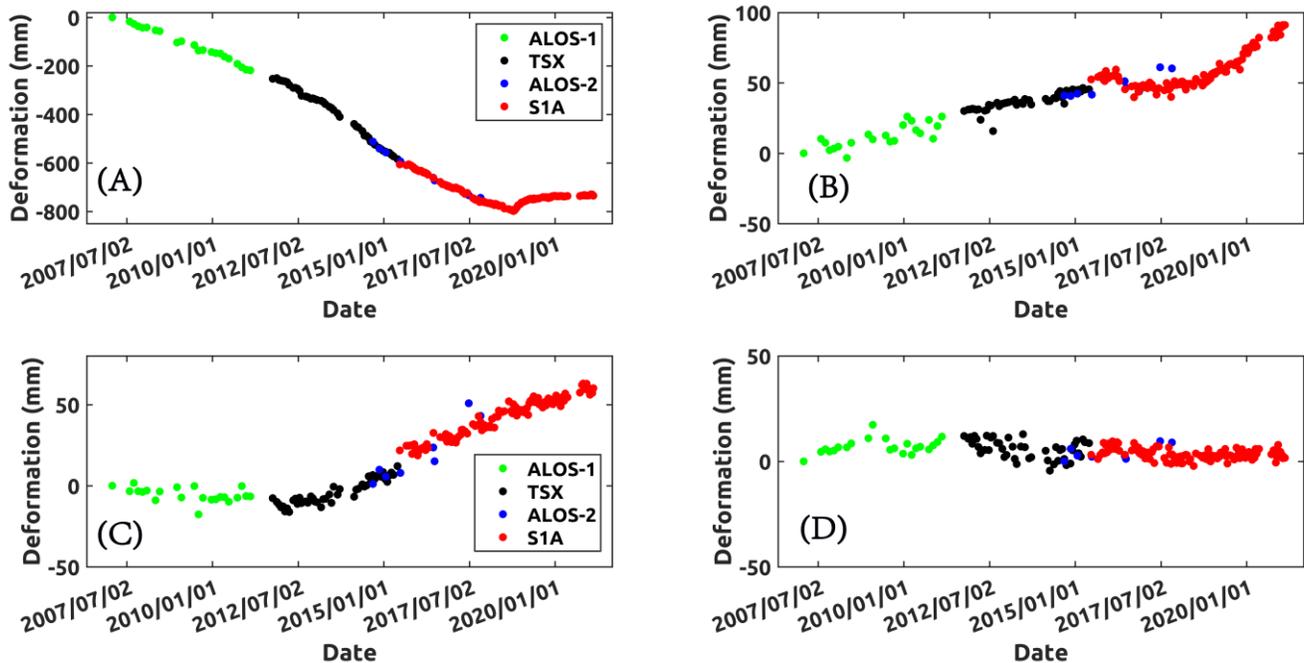


Fig. 11. Time series deformation (A)–(D). The four points are selected to show evolution of uplift deformation.

According to the spatial deformation characteristics shown in Fig. 10, we selected four feature points to show evolution of deformation from January 3, 2007 to February 12, 2021 (Fig.

11). The time series of point A shows a pattern of decline followed by rebound, with a decreasing magnitude of rebound deformation. The deformation time series of point B shows

slow surface deformation prior to 2007. At point C, uplift deformation started in approximately 2012. Point D exemplifies the stable areas.

The contours of confined water in 1960, 1968, 1977, 1983, 1995, and 2004 are mapped in Fig. 12. The rectangular range represents the city wall of Xi'an. From 1960 to 2004, a funnel of declining groundwater level is seen. In 1960, the confined water in the Xi'an area flowed from south to north. The hydraulic gradient was 2-3 %, and the confined water level depth was 10-20 m. In 1968, exploitation of groundwater began and the groundwater flow began to shift, but no funnel of groundwater level decline was found. In 1977, a large amount of confined water was exploited. Three confined water level funnels appeared, and the confined water level dropped to 30-40 m. In 1983, the confined water level funnels

continued to expand. In 1995, the funnel of groundwater level decline reached its maximum and the lowest depth of confined water level exceeded 100 meters.

In 2004, the groundwater level began to rise. Since groundwater exploitation has ceased, we can expect the gradual recovery of the confined groundwater level in Xi'an, accompanied by elastic recovery deformation and time-dependent visco-elastic recovery deformation [69]. The uplift deformation areas in Fig. 10 are consistent with the funnel of groundwater level [70]. As the confined water level continues to move closer to the surface, uplift deformation is inevitable. Uplift deformation is a process of interaction among ground fissures, faults, and groundwater.

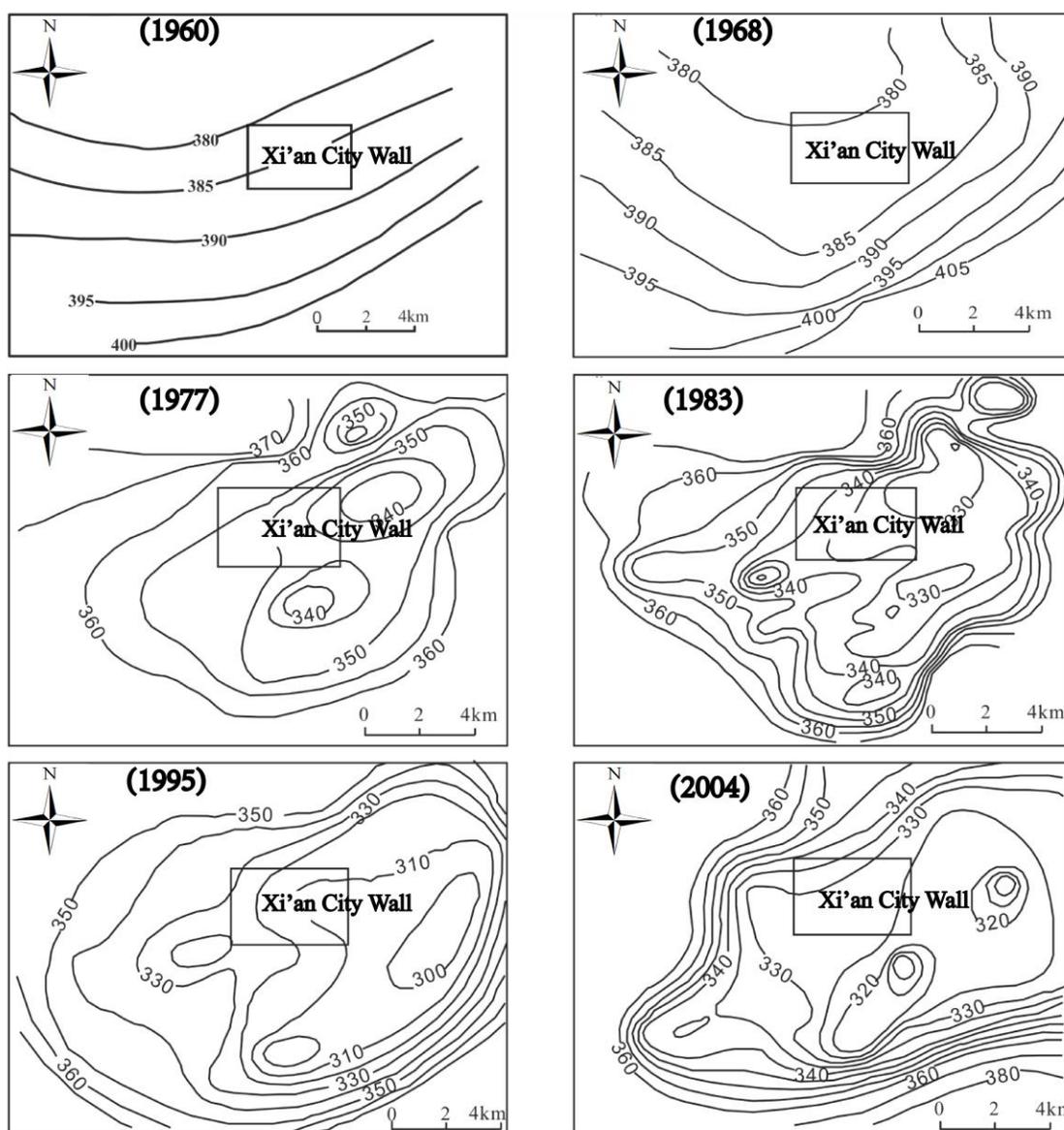


Fig. 12. Contour map of confined water from 1960 to 2004 [70].

Since 1996, Yuhuazhai has experienced the most severe deformation seen in the study area. From 1996 to 2016, the

accumulated land subsidence in this area reached 1.8-2 m [71]. However, the land subsidence stopped suddenly in

mid-October 2018 and rebounded over 130 mm. This was because of artificial water injection in combination with halting exploitation of groundwater at more than 45 deep wells. Due to the larger difference in phreatic aquifer head on both sides of the ground fissure at Yuhazhai, the water injection allowed groundwater to the south of the fissure to recover rapidly. This can be interpreted as immediate elastic recovery deformation [40,69]. Fig. 13 shows that the deformation has tended to be stable since then.

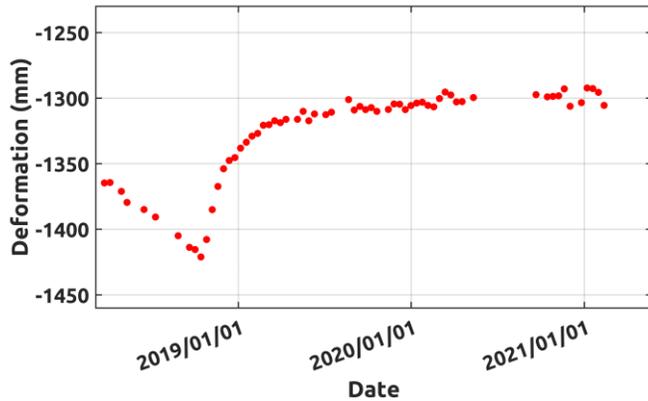


Fig. 13. Rebound deformation time series.

V. CONCLUSION

Both the initial occurrence and evolution of land subsidence in the Xi'an area of China are closely related to groundwater levels. We introduced a long-term continuously updating multi-sensor InSAR deformation time series algorithm to study land subsidence in Xi'an from 2007 to 2021. We found that the Yuhazhai area has tended to be stable since late 2018, ending severe deformation processes of the preceding two and a half decades. We also found a decline in the deformation rate of other areas experiencing land subsidence. We identified a large area of uplift deformation in response to water level recovery. In the future, we can expect to see uplift deformation across a large area in Xi'an. Our proposed approach is an effective tool to continuously update long-term studies in near-real-time using one- or multi-dimensional deformation time series, leveraging the massive quantities of multi-sensor and multi-track SAR data. This approach can significantly improve the temporal resolution of deformation and potentially provide early warning of geohazard disasters.

VI. ACKNOWLEDGMENT

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